

AFRICAN INSTITUTE FOR MATHEMATICAL SCIENCES SCHOOLS ENRICHMENT CENTRE (AIMSSEC)

AIMING HIGH



HELP

Draw the other two radii from the centre of the circle to the points of contact between the circle and the triangle. Imagine splitting the triangle into 3 smaller triangles each of height r and each having one of their vertices at O. Draw this into your diagram.

NEXT a challenge for older learners



You could go up a dimension and investigate the ratios of the volumes and surface areas for a sphere inscribed in a tetrahedron, just touched by the 4 faces of the tetrahedron.

Or you might investigate similar ratios for other polygons.

HOME LEARNING GUIDE



Imagine the triangle split into 3 smaller triangles, each of height r, with bases a, b and c.

Total area of triangle = $\frac{1}{2}(a + b + c)r$

Area of circle = πr^2

Perimeter of triangle = (a + b + c)

Circumference of circle = $2\pi r$

 $\frac{\text{Area of triangle}}{\text{Area of circle}} = \frac{\text{Perimeter of triangle}}{\text{Perimeter of circle}}$

$$= \frac{a+b+c}{2\pi r}$$

of circle = Perimeter of triangle

 $\frac{2}{r}$

 $\frac{Perimeter of circle}{Area of circle} = \frac{Perimeter of triang}{Area of triangle}$



A sphere of radius *r*, centre O, is inscribed in a tetrahedron which has faces of areas *a*, *b*, *c* and *d*.

Imagine the tetrahedron split into 4 smaller tetrahedra, each of height r, with bases a, b, c and d and vertex O.

Total surface area of tetrahedron = (a + b + c + d)

Surface area of sphere = $4\pi r^2$

Total volume of tetrahedron $=\frac{r}{3}(a+b+c+d)$

Volume of sphere = $\frac{4}{3}\pi r^3$

Volume of tetrahedron =Surface area of tetrahedronVolume of sphereSurface area of sphere

$$= \frac{a+b+c+d}{4\pi r^2}$$
Surface area of sphere = Surface area of tetrahedron
Volume of sphere = $\frac{3}{r}$

DIAGNOSTIC ASSESSMENT

This should take about 5–10 minutes.

Show the question to the learners and say:





1. Notice how the learners respond. Ask learner to explain why they gave their answers and DO NOT say whether it is right or wrong but simply thank the learner for giving the answer.

2. It is important for learners to explain the reason for their answer because it helps them to clarify their own thinking and to develop communication skills.

3. If you have a group, try to make sure that learners listen to these reasons and try to decide if their own answer was right or wrong.

4. Ask the learners again to vote for the right answer by putting up 1, 2, 3 or 4 fingers. Notice if there is a change and who gave right and wrong answers.

The correct answer is: B

Possible misconceptions:

A. The learner has misused the formula and not halved the sum of the parallel edges.

- **C**. Could be randomly working out 6×5
- **D**. Could be randomly working out 8×5

https://diagnosticquestions.com

Why do this activity?

This activity gives practice in working out areas of polygons and circles and in working with ratios. For older students the activity could also give practice in working with surface areas and volumes of polyhedra and spheres.

Learning objectives

In doing this activity students will have an opportunity to:

- revise methods of calculating areas and perimeters;
- revise surface areas and volumes of polyhedra and spheres (for older students);
- revise ratios.

Generic competences

In doing this activity students will have an opportunity to **think flexibly**, be creative and innovative and apply knowledge.

Suggestions for Home Learning

You may want to start with the Diagnostic Quiz to check that learners can work out areas. Make sure that they can find the area of the trapezium by splitting it into a triangle and a rectangle as well as just using the formula that they may have learned by rote and understand poorly.

Students need practice in reading comprehension. They need to read questions for themselves and to work independently. Just give out the worksheet from page 1 and tell the learners to work independently.

You can give out the HELP slips to students who struggle to get started. Older students who have met surface areas and volumes of polyhedra and spheres can be given the NEXT slips when they finish the first part.

If you are working with a group then, you can get students to explain their methods to the rest of the group.

You might discuss whether you expected these results. Did you expect the ratios to be the same?

Key questions

- Can you work out the perimeter of the triangle?
- Can you work out the perimeter of the circle?
- Can you think of another name for circumference?
- Can you work out the area of the triangle?
- Can you work out the area of the circle?
- Have you written the ratio in its lowest terms?
- Is there something you can cancel (or divide by) there?
- What is the total surface area of the tetrahedron?
- What is the surface area of the sphere?
- What is total volume of the tetrahedron?
- What is the volume of the sphere?

Follow up

The circle and the square <u>https://aiminghigh.aimssec.ac.za/years-6-8-the-circle-and-the-square/</u> What's the area? <u>https://aiminghigh.aimssec.ac.za/whats-the-area/</u> Can you help these farmers? <u>https://aiminghigh.aimssec.ac.za/years-6-8-can-you-help-these-farmers/</u>

Note: The Grades or School Years specified on the AIMING HIGH Website correspond to Grades 4 to 12 in South Africa and the				
USA, to Years 4 to 12 in the UK and up to Secondary 5 in East Africa. New material will be added for Secondary 6.				
For resources for teaching A level mathematics see <u>https://nrich.maths.org/12339</u>				
Note: The mathematics taught in Year 13 (UK) and Secondary 6 (East Africa) is beyond the school curriculum for Grade 12 SA.				
	Lower Primary	Upper Primary	Lower Secondary	Upper Secondary
	Age 5 to 9	Age 9 to 11	Age 11 to 15	Age 15+
South Africa	Grades R and 1 to 3	Grades 4 to 6	Grades 7 to 9	Grades 10 to 12
USA	Kindergarten and G1 to 3	Grades 4 to 6	Grades 7 to 9	Grades 10 to 12
UK	Reception and Years 1 to 3	Years 4 to 6	Years 7 to 9	Years 10 to 13
East Africa	Nursery and Primary 1 to 3	Primary 4 to 6	Secondary 1 to 3	Secondary 4 to 6